

Units, Dimension, Measurements and Practical Physics

Fundamental or base quantities

The quantities which do not depend upon other quantities for their complete definition are known as *fundamental or base quantities*.

e.g. : length, mass, time, etc.

Derived quantities

The quantities which can be expressed in terms of the fundamental quantities are known as *derived quantities*.

e.g. Speed (=distance/time), volume, acceleration, force, pressure, etc.

Units of physical quantities

The chosen reference standard of measurement in multiples of which, a physical quantity is expressed is called the *unit* of that quantity.

e.g. Physical Quantity = Numerical Value × Unit

Systems of Units

	MKS	CGS	FPS	MKSQ	MKSA
(i)	Length (m)	Length (cm)	Length (ft)	Length (m)	Length (m)
(ii)	Mass (kg)	Mass (g)	Mass (pound)	Mass (kg)	Mass (kg)
(iii)	Time (s)	Time (s)	Time (s)	Time (s)	Time (s)
(iv)	-	-	-	Charge (Q)	Current (A)

Fundamental Quantities in S.I. System and their units

S.N.	Physical Qty.	Name of Unit	Symbol
1	Mass	kilogram	kg
2	Length	meter	m
3	Time	second	s
4	Temperature	kelvin	K
5	Luminous intensity	candela	Cd
6	Electric current	ampere	A
7	Amount of substance	mole	mol

SI Base Quantities and Units

Base Quantity	SI Units		
	Name	Symbol	Definition
Length	meter	m	The meter is the length of the path traveled by light in vacuum during a time interval of $1/(299, 792, 458)$ of a second (1983)
Mass	kilogram	kg	The kilogram is equal to the mass of the international prototype of the kilogram (a platinum-iridium alloy cylinder) kept at International Bureau of Weights and Measures, at Sevres, near Paris, France. (1889)
Time	second	s	The second is the duration of 9, 192, 631, 770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the cesium-133 atom (1967)
Electric Current	ampere	A	The ampere is that constant current which, if maintained in two straight parallel conductors of infinite length, of negligible circular cross-section, and placed 1 metre apart in vacuum, would produce between these conductors a force equal to 2×10^{-7} Newton per metre of length. (1948)
Thermodynamic Temperature	kelvin	K	The kelvin, is the fraction $1/273.16$ of the thermodynamic temperature of the triple point of water. (1967)
Amount of Substance	mole	mol	The mole is the amount of substance of a system, which contains as many elementary entities as there are atoms in 0.012 kilogram of carbon-12. (1971)
Luminous Intensity	candela	Cd	The candela is the luminous intensity, in a given direction, of a source that emits monochromatic radiation of frequency 540×10^{12} hertz and that has a radiant intensity in that direction of $1/683$ watt per steradian (1979).

Supplementary Units

- Radian (rad) - for measurement of plane angle
- Steradian (sr) - for measurement of solid angle

Dimensional Formula

Relation which express physical quantities in terms of appropriate powers of fundamental units.

Use of dimensional analysis

- To check the dimensional correctness of a given physical relation
- To derive relationship between different physical quantities
- To convert units of a physical quantity from one system to another

$$n_1 u_1 = n_2 u_2 \Rightarrow n_2 = n_1 \left(\frac{M_1}{M_2} \right)^a \left(\frac{L_1}{L_2} \right)^b \left(\frac{T_1}{T_2} \right)^c$$

where $u = M^a L^b T^c$

Limitations of dimensional analysis

- In Mechanics the formula for a physical quantity depending on more than three other physical quantities cannot be derived. It can only be checked.
- This method can be used only if the dependency is of multiplication type. The formulae containing exponential, trigonometrical and logarithmic functions can't be derived using this method. Formulae containing more than one term which are added or subtracted like $s = ut + \frac{1}{2} at^2$ also can't be derived.
- The relation derived from this method gives no information about the dimensionless constants.
- If dimensions are given, physical quantity may not be unique as many physical quantities have the same dimensions.
- It gives no information whether a physical quantity is a scalar or a vector.

SI PREFIXES

The magnitudes of physical quantities vary over a wide range. The CGPM recommended standard prefixes for magnitude too large or too small to be expressed more compactly for certain powers of 10.

**PREFIXES
USED FOR
DIFFERENT
POWERS
OF 10**

Power of 10	Prefix	Symbol	Power of 10	Prefix	Symbol
10^{18}	exa	E	10^{-1}	deci	d
10^{15}	peta	P	10^{-2}	centi	c
10^{12}	tera	T	10^{-3}	milli	m
10^9	giga	G	10^{-6}	micro	μ
10^6	mega	M	10^{-9}	nano	n
10^3	kilo	k	10^{-12}	pico	p
10^2	hecto	h	10^{-15}	femto	f
10^1	deca	da	10^{-18}	atto	a

**UNITS
OF
IMPORTANT
PHYSICAL
QUANTITIES**

Physical quantity	Unit	Physical quantity	Unit
Angular acceleration	rad s ⁻²	Frequency	hertz
Moment of inertia	kg - m ²	Resistance	kg m ² A ⁻² s ⁻³
Self inductance	henry	Surface tension	newton/m
Magnetic flux	weber	Universal gas constant	joule K ⁻¹ mol ⁻¹
Pole strength	A-m	Dipole moment	coulomb-meter
Viscosity	poise	Stefan constant	watt m ⁻² K ⁻⁴
Reactance	ohm	Permittivity of free space (ϵ_0)	coulomb ² /N-m ²
Specific heat	J/kg°C	Permeability of free space (μ_0)	weber/A-m
Strength of magnetic field	newton A ⁻¹ m ⁻¹	Planck's constant	joule-sec
Astronomical distance	Parsec	Entropy	J/K

DIMENSIONS OF IMPORTANT PHYSICAL QUANTITIES

Physical quantity	Dimensions	Physical quantity	Dimensions
Momentum	$M^1 L^1 T^{-1}$	Capacitance	$M^{-1} L^{-2} T^4 A^2$
Calorie	$M^1 L^2 T^{-2}$	Modulus of rigidity	$M^1 L^{-1} T^{-2}$
Latent heat capacity	$M^0 L^2 T^{-2}$	Magnetic permeability	$M^1 L^1 T^{-2} A^{-2}$
Self inductance	$M^1 L^2 T^{-2} A^{-2}$	Pressure	$M^1 L^{-1} T^{-2}$
Coefficient of thermal conductivity	$M^1 L^1 T^{-3} K^{-1}$	Planck's constant	$M^1 L^2 T^{-1}$
Power	$M^1 L^2 T^{-3}$	Solar constant	$M^1 L^0 T^{-3}$
Impulse	$M^1 L^1 T^{-1}$	Magnetic flux	$M^1 L^2 T^{-2} A^{-1}$
Hole mobility in a semi conductor	$M^{-1} L^0 T^2 A^1$	Current density	$M^0 L^{-2} T^0 A^1$
Bulk modulus of elasticity	$M^1 L^{-1} T^{-2}$	Young modulus	$M^1 L^{-1} T^{-2}$
Potential energy	$M^1 L^2 T^{-2}$	Magnetic field intensity	$M^0 L^{-1} T^0 A^1$
Gravitational constant	$M^{-1} L^3 T^{-2}$	Magnetic Induction	$M^1 T^{-2} A^{-1}$
Light year	$M^0 L^1 T^0$	Electric Permittivity	$M^{-1} L^{-3} T^4 A^2$
Thermal resistance	$M^{-1} L^{-2} T^3 K$	Electric Field	$M^1 L^1 T^{-3} A^{-1}$
Coefficient of viscosity	$M^1 L^{-1} T^{-1}$	Resistance	$M L^2 T^{-3} A^{-2}$

SETS OF QUANTITIES HAVING SAME DIMENSIONS

S.N.	Quantities	Dimensions
1.	Strain, refractive index, relative density, angle, solid angle, phase, distance gradient, relative permeability, relative permittivity, angle of contact, Reynolds number, coefficient of friction, mechanical equivalent of heat, electric susceptibility, etc.	$[M^0 L^0 T^0]$
2.	Mass or inertial mass	$[M^1 L^0 T^0]$
3.	Momentum and impulse.	$[M^1 L^1 T^{-1}]$
4.	Thrust, force, weight, tension, energy gradient.	$[M^1 L^1 T^{-2}]$
5.	Pressure, stress, Young's modulus, bulk modulus, shear modulus, modulus of rigidity, energy density.	$[M^1 L^{-1} T^{-2}]$
6.	Angular momentum and Planck's constant (h).	$[M^1 L^2 T^{-1}]$
7.	Acceleration, g and gravitational field intensity.	$[M^0 L^1 T^{-2}]$
8.	Surface tension, free surface energy (energy per unit area), force gradient, spring constant.	$[M^1 L^0 T^{-2}]$
9.	Latent heat capacity and gravitational potential.	$[M^0 L^2 T^{-2}]$
10.	Thermal capacity, Boltzmann constant, entropy.	$[M L^2 T^{-2} K^{-1}]$
11.	Work, torque, internal energy, potential energy, kinetic energy, moment of force, (q^2/C) , (LI^2) , (qV) , (V^2C) , (I^2Rt) , $\frac{V^2}{R}t$, (VI) , (PV) , (RT) , (mL) , $(mc \Delta T)$	$[M^1 L^2 T^{-2}]$
12.	Frequency, angular frequency, angular velocity, velocity gradient, radioactivity $\frac{R}{L}, \frac{1}{RC}, \frac{1}{\sqrt{LC}}$	$[M^0 L^0 T^{-1}]$
13.	$\left(\frac{l}{g}\right)^{1/2}, \left(\frac{m}{k}\right)^{1/2}, \left(\frac{L}{R}\right), (RC), (\sqrt{LC})$, time	$[M^0 L^0 T^1]$
14.	(VI) , (I^2R) , (V^2/R) , Power	$[M L^2 T^{-3}]$

SOME FUNDAMENTAL CONSTANTS

Gravitational constant (G)	$6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$
Speed of light in vacuum (c)	$3 \times 10^8 \text{ ms}^{-1}$
Permeability of vacuum (μ_0)	$4\pi \times 10^{-7} \text{ H m}^{-1}$
Permittivity of vacuum (ϵ_0)	$8.85 \times 10^{-12} \text{ F m}^{-1}$
Planck constant (h)	$6.63 \times 10^{-34} \text{ Js}$
Atomic mass unit (amu)	$1.66 \times 10^{-27} \text{ kg}$
Energy equivalent of 1 amu	931.5 MeV
Electron rest mass (m_e)	$9.1 \times 10^{-31} \text{ kg} \approx 0.511 \text{ MeV}$
Avogadro constant (N_A)	$6.02 \times 10^{23} \text{ mol}^{-1}$
Faraday constant (F)	$9.648 \times 10^4 \text{ C mol}^{-1}$
Stefan-Boltzmann constant (σ)	$5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$
Wien constant (b)	$2.89 \times 10^{-3} \text{ mK}$
Rydberg constant (R_∞)	$1.097 \times 10^7 \text{ m}^{-1}$
Triple point for water	273.16 K (0.01°C)
Molar volume of ideal gas (NTP)	$22.4 \text{ L} = 22.4 \times 10^{-3} \text{ m}^3 \text{ mol}^{-1}$

KEY POINTS

- Trigonometric functions $\sin\theta$, $\cos\theta$, $\tan\theta$ etc and their arrangements θ are dimensionless.
- Dimensions of differential coefficients $\left[\frac{d^ny}{dx^n}\right] = \left[\frac{y}{x^n}\right]$
- Dimensions of integrals $\left[\int ydx\right] = [yx]$
- We can't add or subtract two physical quantities of different dimensions.
- Independent quantities may be taken as fundamental quantities in a new system of units.

PRACTICAL PHYSICS

Rules for Counting Significant Figures

For a number greater than 1

- All non-zero digits are significant.
- All zeros between two non-zero digits are significant. Location of decimal does not matter.
- If the number is without decimal part, then the terminal or trailing zeros are not significant.
- Trailing zeros in the decimal part are significant.

For a Number Less than 1

Any zero to the right of a non-zero digit is significant. All zeros between decimal point and first non-zero digit are not significant.

Significant Figures

All accurately known digits in measurement plus the first uncertain digit together form significant figure.

Ex. 0.108 → 3SF, 40.000 → 5SF,
1.23 × 10⁻¹⁹ → 3SF, 0.0018 → 2SF

Significant Digits

The product or quotient will be reported as having as many significant digits as the number involved in the operation with the least number of significant digits.

For example : $0.000170 \times 100.40 = 0.017068$
Another example : $2.000 \times 10^4 / 6.0 \times 10^{-3} = 0.33 \times 10^7$

For example : $3.0 \times 800.0 = 2.4 \times 10^3$

The sum or difference can be no more precise than the least precise number involved in the mathematical operation. Precision has to do with the number of positions to the RIGHT of the decimal. The more position to the right of the decimal, the more precise the number. So a sum or difference can have no more indicated positions to the right of the decimal as the number involved in the operation with the LEAST indicated positions to the right of its decimal. For example : $160.45 + 6.732 = 167.18$ (after rounding off)

Another example : $45.621 + 4.3 - 6.41 = 43.5$ (after rounding off)

Rules for rounding off digits :

1. If the digit to the right of the last reported digit is less than 5 round it and all digits to its right off.
2. If the digit to the right of the last reported digit is greater than 5 round it and all digits to its right off and increased the last reported digit by one.
3. If the digit to the right of the last reported digit is a 5 followed by either no other digits or all zeros, round it and all digits to its right off and if the last reported digit is odd round up to the next even digit. If the last reported digit is even then leave it as is.

For example if we wish to round off the following number to 3 significant digits : 18.3682

The answer is : 18.4. Another example : Round off 4.565 to three significant digits.

The answer would be 4.56.

Rounding off

6.87 → 6.9, 6.84 → 6.8, 6.85 → 6.8,
6.75 → 6.8, 6.65 → 6.6, 6.95 → 7.0

Order of magnitude

Power of 10 required to represent a quantity

$49 = 4.9 \times 10^1 \approx 10^1 \Rightarrow$ order of magnitude = 1

$51 = 5.1 \times 10^1 \approx 10^2 \Rightarrow$ order of magnitude = 2

$0.051 = 5.1 \times 10^{-2} \approx 10^{-1}$ order of magnitude = -1

Errors

Whenever an experiment is performed, two kinds of errors can appear in the measured quantity.

(1) random and (2) systematic errors.

1. Random errors appear randomly because of operator, fluctuations in external conditions and variability of measuring instruments. The effect of random error can be somewhat reduced by taking the average of measured values. Random errors have no fixed sign or size.
2. Systematic errors occur due to error in the procedure, or miscalibration of the instrument etc. Such errors have same size and sign for all the measurements. Such errors can be determined.

A measurement with relatively small random error is said to have high precision. A measurement with small random error and small systematic error is said to have high accuracy.

Least Count Error :- If the instrument has known least count, the absolute error is taken to be equal to the least count unless otherwise stated.

Relative error = $\frac{\text{absolute error in a measurement}}{\text{size of the measurement}}$

A. Systematic errors:

They have a known sign. The systematic error is removed before beginning calculations. Bench error and zero error are examples of systematic error.

Propagation of combination of errors

Error in Summation and Difference :

$x = a + b$ then $\Delta x = \pm (\Delta a + \Delta b)$

Error in Product and Division

A physical quantity X depend upon Y & Z as $X = Y^a Z^b$ then maximum possible fractional error in X.

$$\frac{\Delta X}{X} = |a| \frac{\Delta Y}{Y} + |b| \frac{\Delta Z}{Z}$$

Error in Power of a Quantity

$$x = \frac{a^m}{b^n} \text{ then } \frac{\Delta x}{x} = \pm \left[m \left(\frac{\Delta a}{a} \right) + n \left(\frac{\Delta b}{b} \right) \right]$$

The quotient rule is not applicable if the numerator and denominator are dependent on each other.

e.g if $R = \frac{XY}{X+Y}$. We cannot apply quotient rule

to find the error in R. Instead we write the equation

as follows $\frac{1}{R} = \frac{1}{X} + \frac{1}{Y}$. Differentiating both

the sides, we get $-\frac{dR}{R^2} = -\frac{dX}{X^2} - \frac{dY}{Y^2}$.

$$\text{Thus } \frac{r}{R^2} = \frac{x}{X^2} + \frac{y}{Y^2}$$

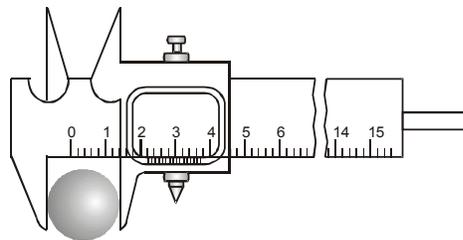
Least count

The smallest value of a physical quantity which can be measured accurately with an instrument is called the least count of the measuring instrument.

Vernier Callipers

Least count = 1MSD - 1VSD

(MSD → main scale division, VSD → Vernier scale division)

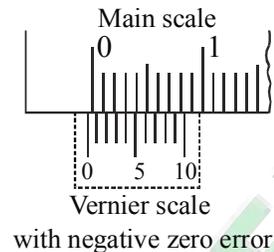
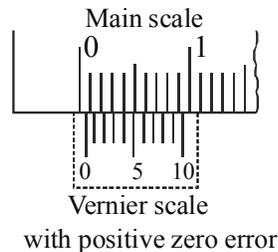
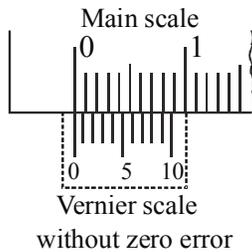


Ex. A vernier scale has 10 parts, which are equal to 9 parts of main scale having each part equal to 1

mm then least count = $1 \text{ mm} - \frac{9}{10} \text{ mm} = 0.1 \text{ mm}$

[∴ 9 MSD = 10 VSD]

Zero Error



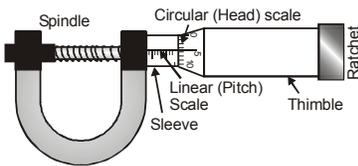
(i)

(ii)

The zero error is always subtracted from the reading to get the corrected value.
If the zero error is positive, its value is calculated as we take any normal reading.
Negative zero error = - [Total no. of vsd - vsd coinciding] × L.C.

Screw Gauge

$$\text{Least count} = \frac{\text{pitch}}{\text{total no. of divisions on circular scale}}$$



Ex. The distance moved by spindle of a screw gauge for each turn of head is 1mm. The edge of the thimble is

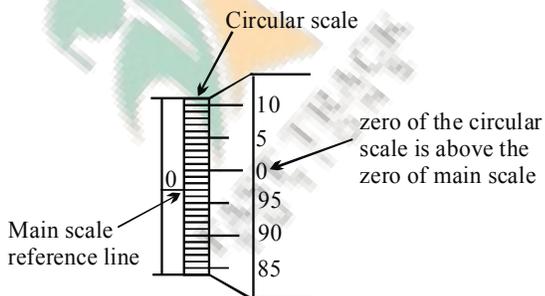
provided with an angular scale carrying 100 equal divisions. The least count = $\frac{1\text{mm}}{100} = 0.01 \text{ mm}$

Zero Error

If there is no object between the jaws (i.e. jaws are in contact), the screw gauge should give zero reading. But due to extra material on jaws, even if there is no object, it gives some excess reading. This excess reading is called Zero error.

Negative Zero Error

(3 division error) i.e., -0.003 cm



Positive Zero Error

(2 division error) i.e., +0.002 cm

